

TECHNICAL REPORT CR-RD-PR-88-1

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**PRELIMINARY INVESTIGATION OF FLOW MODELING  
DURING SOLID PROPELLANT PROCESSING**

H. M. Dornanus  
W. T. Sha  
Analytical Thermal Hydraulic Research Program  
Argonne National Laboratory  
Argonne, Illinois 60439

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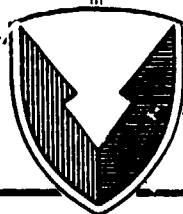
S. L. Soo  
Department of Mechanical and Industrial Engineering  
University of Illinois-Urbana  
Urbana, Illinois 61801

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by

H. M. Domanus  
W. T. Sha  
Analytical Thermal Hydraulic Research Program  
Materials and Components Technology Division  
Argonne National Laboratory  
9700 South Cass Avenue  
Argonne, Illinois 60439

and

S. L. Soo  
Department of Mechanical and Industrial Engineering  
University of Illinois-Urbana  
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## 1. OBJECTIVE

The objective of the proposed work is to develop a computer model capable of predicting the distribution of solid particle constituents during the processing of solid propellants.

## 2. INTRODUCTION

In order to control the propellant burning rate and, hence, the propulsive performance of a solid rocket motor, it is essential to create a desired particle distribution throughout a solid propellant. It is therefore desirable to determine, via computation, the distribution of particulates during the casting of solid rocket fuel. The present program, fundamental in nature, is geared toward initiating, understanding, and modeling the mechanisms that control the distribution of solid particle constituents during the processing of a solid propellant.

The propellant casting can be considered as a multiphase flow process with a dense suspension fluid in creeping motion. In such a case, the shear resistance (shear lift phenomenon), relaxation phenomenon due to particle-particle interaction, particle-fluid interaction, and particle-wall interaction predominate even though the fluid phase (binders) may be serving the main function of transporting. Even if we start with a uniform mix of particles of various sizes, non-uniformity may result from:

- (1) particle-fluid interactions alone - small particles due to shear lift force tend to move away from the wall faster than large particles.
- (2) particle-particle interactions alone - small particles tend to act as a fluid, exerting a shear lift force on the large particles. The large particles tend to move away from the wall faster than the small particles.

- (3) the boundary condition at the wall where the fluid velocity must be zero, but the particle velocity may have a finite value (slip motion). Thus, particles tend to migrate toward the center of the passage or away from the wall.

These expected facts[1] are in agreement with observation by Bradfield[2] of WRE (Weapons Research Establishment).

In treating the present problem of transient flow with solids of various particle sizes in a liquid suspension, we need to consider:

- (1) shear lift phenomenon,
- (2) particle-particle interaction,
- (3) particle-fluid interactions, and
- (4) particle-wall interactions.

The shear lift phenomenon of solid particles in a fluid was formulated by Saffman[3], studied experimentally by Segré and Silberberg[4], and correlated by Soo[5], including the resultant concentration in steady or depositing flow[6]. The effect of particle diffusivity was found to be important. Segré and Silberberg[4] particularly identified that in laminar pipe flow of a suspension of neutral buoyancy, the maximum concentration of particles tends to occur at  $2/3$  radius from the pipe axis, that is, toward the wall, than toward the center. Many of these basic relations concerning the distribution of particulates in a fluid need to be synthesized and formulated for the present system.

It should be noted that very little work has been done, both experimentally and theoretically, on dense suspension systems.

### **3. MATHEMATICAL MODELING**

#### **3.1 Multiple Velocity Field Model or Multifluid Model**

Use of a multiple velocity field model calls for a set of formulations including continuity and momentum equations of phases, or in the present case,

components. The continuity equations are

$$\frac{\partial \theta_1 \rho_1}{\partial t} + \nabla \cdot (\theta_1 \rho_1 \underline{U}_1) = 0 \quad (1)$$

$$\frac{\partial \theta_2 \rho_2}{\partial t} + \nabla \cdot (\theta_2 \rho_2 \underline{U}_2) = 0 \quad (2)$$

$$\frac{\partial \theta_3 \rho_3}{\partial t} + \nabla \cdot (\theta_3 \rho_3 \underline{U}_3) = 0 \quad (3)$$

where  $\theta_1$ ,  $\rho_1$ ,  $\underline{U}_1$  refer to the volume fraction, the material density, and the velocity of the binder; subscripts 2 refer to the aluminum powder and 3 refers to the ammonium perchlorate powder. For the example of  $\theta_1 = 0.2352$ ,  $\theta_2 = 0.1269$ , and  $\theta_3 = 0.6379$ , noting that  $\theta_1 + \theta_2 + \theta_3 = 1$ . The momentum equations are

$$\begin{aligned} \frac{\partial \theta_1 \rho_1 \underline{U}_1}{\partial t} + \nabla \cdot (\theta_1 \rho_1 \underline{U}_1 \underline{U}_1) = & -\theta_1 \nabla P + \nabla \cdot \underline{\tau}_{1m} + \theta_1 \rho_1 \underline{f}_1 - K_{12}(\underline{U}_1 - \underline{U}_2) \\ & - K_{13}(\underline{U}_1 - \underline{U}_3) \end{aligned} \quad (4)$$

$$\begin{aligned} \frac{\partial \theta_2 \rho_2 \underline{U}_2}{\partial t} + \nabla \cdot (\theta_2 \rho_2 \underline{U}_2 \underline{U}_2) = & -\theta_2 \nabla P + \nabla \cdot \underline{\tau}_{2m} + \theta_2 \rho_2 \underline{f}_2 - K_{21}(\underline{U}_2 - \underline{U}_1) \\ & - K_{23}(\underline{U}_2 - \underline{U}_3) \end{aligned} \quad (5)$$

$$\begin{aligned} \frac{\partial \theta_3 \rho_3 \underline{U}_3}{\partial t} + \nabla \cdot (\theta_3 \rho_3 \underline{U}_3 \underline{U}_3) = & -\theta_3 \nabla P + \nabla \cdot \underline{\tau}_{3m} + \theta_3 \rho_3 \underline{f}_3 - K_{31}(\underline{U}_3 - \underline{U}_1) \\ & - K_{32}(\underline{U}_3 - \underline{U}_2) \end{aligned} \quad (6)$$

where  $P$  is the pressure,  $\tau_{1m}$  is the shear stress of component 1 in the mixture,  $\underline{f}_1$  is the field force per unit mass on component 1 and may include that due to the shear lift effect\*.  $K_{12}$  is the interfacial momentum transfer coefficient including drag between phase 2 and phase 1, etc., where

---

\*The magnitude of shear lift here is seen not to be influenced by the rotation of the particles[3].

$$K_{12} = \theta_1 \rho_1 F_{12}, \text{ etc.}$$

$F_{12}$  is the inverse relaxation time for momentum transfer from phase 2 to phase 1, etc., and

$$\theta_1 \rho_1 F_{12} = \theta_2 \rho_2 F_{21} \quad \text{or} \quad K_{12} = K_{21}$$

etc. from action and reaction. With correct boundary conditions, Eqs. 1 to 6 are solved for an isothermal system to determine the volume fraction and velocity distribution of phases. Transport properties are needed to determine  $\tau_{lm}$  etc. and  $F_{12}$  etc.  $F_{12}$ ,  $F_{21}$ ,  $F_{13}$ , and  $F_{31}$  arise from fluid-particle interaction.  $F_{23}$  or  $F_{32}$  arises from particle-particle interaction. These quantities depend on the properties of materials and operating conditions; non-Newtonian behaviors are expected for the present system.

For given initial conditions, pertinent boundary conditions for the above equation for flow through a pipe of radius  $R$  include

$$r = R, \quad U_{1z} = 0$$

$$U_{2z} = -L_{21} \left. \frac{\partial U_{2z}}{\partial r} \right|_R$$

$$U_{3z} = -L_{31} \left. \frac{\partial U_{3z}}{\partial r} \right|_R$$

for the axial velocities, where  $L_{21}$  is the interaction length of particle to fluid, leading to slip motion and  $L_{21} = \left\langle (\Delta u)_{21}^2 \right\rangle^{1/2} / F_{21}$  where  $\left\langle (\Delta u)_{21}^2 \right\rangle^{1/2}$  is the relative intensity of motion of phase 2 in 1, and  $F_{21}$  can be large for small particles in a viscous fluid. A limiting case will be

$$\partial U_{2z} / \partial r = \partial U_{3z} / \partial r = 0.$$

Since the particulate material finally set in their place by solidification rather than by deposition, the boundary condition for the volume fraction of



particles at the wall is given by [6] ( $k = 2, 3$ )

$$D_{km} \frac{\partial \theta_k}{\partial r} \bigg|_R = \theta_k f_k / F_{kl}$$

While  $\tau_{1m}$  is defined according to the multiphase formulation, its determination for the present system is complicated because of a dense suspension. Based on the theory of dense suspensions[7],  $\tau_{1m}$  is expected to be greater than  $\tau_1$  (pure binder). In general  $\tau_m$  of the mixture is strongly influenced by the perchlorate powder (63% by volume). Unlike the case of a dilute suspension,  $\tau_{1m}$ ,  $\tau_{2m}$ ,  $\tau_{3m}$  are not readily determined at this time. (In the case of dilute suspensions of 2 and 3,  $\tau_{1m} \sim \tau_1$ ,  $\tau_{2m} = D_{2m} \theta_2 \rho_2$ ,  $\tau_{3m} = D_{3m} \theta_3 \rho_3$ ;  $D_{2m}$  is the diffusivity of particles 2 in the mixture. Likewise,  $D_{3m}$  is the diffusivity of particles 3 in the mixture.) In the present case, it suffices to say that  $\tau_{2m} \equiv \mu_{2m} \underline{\Delta}_2$ , where  $\mu_{2m}$  is the viscosity of phase 2 in the mixture,  $\underline{\Delta}_2$  is the deformation tensor of the motion of phase 2, and  $\mu_{2m}$  is related to  $D_{2m}$  according to the relation of a dense suspension[7].

Computations based on the multifluid model calls for simultaneous solution of Eqs. 1 to 6 with pertinent boundary conditions and accurate transport properties  $F_{21}$ ,  $F_{31}$ ,  $F_{32}$  and  $\mu_{1m}$ ,  $\mu_{2m}$ , and  $\mu_{3m}$ . The latter are not readily computed or measured; often the best we can manage is the viscosity of the mixture. The closeness, though different, of the phase velocities also suggests that the mixture velocity may be sufficiently representative. Thus, it leads us to use the relatively simple single velocity field model as described in the following section.

### 3.2 Single Velocity Field Model

Summing Eqs. 4, 5, and 6 gives the momentum equation of the mixture as

$$\frac{\partial \rho_m \underline{U}}{\partial t} + \nabla \cdot (\rho_m \underline{U} \underline{U}) + \nabla \cdot \sum_{k=1,2,3} \theta_k \rho_k (\underline{U}_k - \underline{U})(\underline{U}_k - \underline{U})$$

$$= -\nabla P + \nabla \cdot \underline{\tau}_m + \rho_m \underline{f}_m \quad (7)$$

$\underline{\tau}_m = \mu_m \underline{\Delta}$  while internal action and reaction for momentum transfer cancel each other. The mixture density and velocity are defined by

$$\rho_m = \sum_{k=1,2,3} \theta_k \rho_k$$

and

$$\rho_m \underline{U}_m = \sum_{k=1,2,3} \theta_k \rho_k \underline{U}_k \quad (8)$$

while the field force is given by

$$\rho_m \underline{f}_m = \sum_{k=1,2,3} \theta_k \rho_k \underline{f}_k$$

for  $k = 1, 2, 3$  as in Section 3.1. For a dense mixture, the velocity difference  $(\underline{U}_k - \underline{U}_m)$  is small and the third term on the left side of Eq. 7 can be neglected.

Equations. 2 and 3 can be modified by considering the continuity equation of the mixture obtained from summing Eqs. 1, 2, and 3, or

$$\frac{\partial \rho_m}{\partial t} + \nabla \cdot \rho_m \underline{U}_m = 0. \quad (9)$$

The continuity equation of species  $k$  ( $k = 2, 3$ ) can be rewritten as

$$\frac{\partial \rho_k \theta_k}{\partial t} + \nabla \cdot (\rho_k \theta_k \underline{U}_m) = \nabla \cdot \rho_k \theta_k (\underline{U}_m - \underline{U}_k). \quad (10)$$

Since  $\rho_k \theta_k (\underline{U}_k - \underline{U}_m) = \underline{J}_k$ , the general flux of phase  $k$ , we have

$$\frac{\partial \rho_k \theta_k}{\partial t} + \nabla \cdot (\rho_k \theta_k \underline{U}_m) = -\nabla \cdot \underline{J}_k. \quad (11)$$

or

$$\frac{\partial \rho_k \theta_k}{\partial t} + \underline{U}_m \cdot \nabla \rho_k \theta_k = -\rho_k \theta_k \nabla \cdot \underline{U}_m - \nabla \cdot \underline{J}_k \equiv \frac{d \rho_k \theta_k}{d t_m} \quad (12)$$

In terms of mass fraction  $c_k = \theta_k \rho_k / \rho_m$ , Eq. 11 becomes

$$\frac{\partial \rho_m c_k}{\partial t} + \nabla \cdot (c_k \rho_m \underline{U}_m) = - \nabla \cdot \underline{J}_k . \quad (13)$$

Subtracting the product of  $c_k$  and Eq. 9 from Eq. 13, and rearranging, we get

$$\rho_m \frac{\partial c_k}{\partial t} + \rho_m \underline{U}_m \cdot \nabla c_k = - \nabla \cdot \underline{J}_k \quad (14)$$

or

$$\rho_m \frac{d c_k}{d t_m} = - \nabla \cdot \underline{J}_k . \quad (15)$$

For nearly constant  $\rho_m$ , the component continuity equation takes the form

$$\frac{d \rho_k \theta_k}{d t_m} = \frac{\partial \rho_k \theta_k}{\partial t} + \underline{U}_m \cdot \nabla (\rho_k \theta_k) = - \nabla \cdot \underline{J}_k . \quad (16)$$

Either Eqs. 5 or 6, neglecting inertial forces, pressure gradient, and assuming equal particle velocities and binder velocity approximately equal to the mixture velocity, gives

$$\begin{aligned} \underline{J}_k &= \frac{\theta_k \rho_k \underline{f}_k}{F_{kl}} + \nabla \cdot \left( \frac{\mu_{km}}{F_{kl}} \nabla \underline{U}_k \right) \\ &= \frac{\theta_k \rho_k \underline{f}_k}{F_{kl}} - D_{km} \nabla (\rho_k \theta_k) \end{aligned} \quad (17)$$

for drift by field forces and diffusion by concentration gradient. This is because shear resistance in a suspension arises from resistance to transport of momentum by diffusion. The kinematic viscosity and diffusivity  $D_{km}$ , are related by

$$\frac{\mu_{km}}{F_{kl}} \nabla \underline{U}_k = \frac{\theta_k \rho_k}{F_{kl}} \nu_{km} \nabla \underline{U}_k = - \rho_k \theta_k D_{km} \quad (18)$$

with the correspondence of  $(\nu_{km}/F_{kl}) \nabla \underline{U}_k \sim -D_{km}$ . This correspondence serves to explain the relation between the diffusion model and the multifluid model. It is noted that the diffusion flux is usually derived in a different manner[8]. Equation 16 now reduces for nearly constant  $\rho_m$  to

$$\frac{\partial \rho_k \theta_k}{\partial t} + \underline{U}_m \cdot \nabla (\rho_k \theta_k) = \nabla \cdot [D_{km} \nabla (\theta_k \rho_k) - \frac{f_k \theta_k \rho_k}{F_{kl}}] \quad (19)$$

which is the diffusion equation.

The diffusion equation renders the continuity equation of phase  $k$  independent of its momentum equation. However, once  $\theta_k$  is determined,  $\underline{U}_k$  can still be calculated from its momentum equation if it is needed. Often a knowledge of the distribution of  $\theta_k$  is sufficient. Equations 7, 9, and 19 ( $k = 2, 3$ ) can be solved for  $P$ ,  $\theta_1$ ,  $\theta_2$ ,  $\theta_3$  and  $\underline{U}_m$  for the following boundary conditions:

$$r = R. \quad \underline{U}_m = 0$$

$$- D_{km} \left. \frac{\partial \rho_k \theta_k}{\partial r} \right|_R = - \rho_k \theta_k \frac{f_k}{F_{kl}}$$

for given initial conditions.

It is recognized that  $F_{21}$ ,  $F_{31}$ ,  $F_{32}$ ,  $D_{km}$  and  $\mu_m$  still have to be determined experimentally for accurate prediction.

#### 4. EXPLORATORY CALCULATIONS

In the process of forming a solid propellant motor, several different particulate materials are mixed together with a polymer binder. The batch is mixed until the mixture becomes uniform and homogeneous. The homogeneous mixture is then passed through a network of pipes and ducts to a mold. As the mixture flows, the components of the mixture begin to displace relative to one another by shear motion. This gives rise to non-uniform propellant properties in the mold and hence the final cured motor.

The ability to calculate partial component separation from a homogeneous mixture is a crucial feature which must be present in the mathematical model. In order to investigate and demonstrate that the proposed mathematical model is capable of simulating this separation phenomena, some exploratory calcula-

tions were made for representative situations. The numerical results presented here were obtained with the COMMIX code[9,10], which was modified to carry out these calculations.

#### 4.1 Numerical Model

Flow into a  $6.35\text{E-}3$  m (0.25 in) gap between two parallel plates and into an annulus is considered. A two-velocity field model is used to describe the flow and component distributions. (Component #1 represents the polymer binder and component #2 represents the particles. The governing equations are discretized by the finite volume technique. The two-dimensional computational domain is partitioned into 8 equal partitions across the gap and 20 along the flow direction. The overall length modeled (0.0254 m) was long enough so that the flow would become fully developed. At the entrance, the mixture is assumed to be homogeneous and have a uniform velocity of 0.01 m/s. The binder (component #1) is assumed to stick to the wall ( $v_1|_w = 0$ ), while the particles (component #2) are assumed to have a free slip boundary condition  $\left(\frac{\partial v_2}{\partial x}\right)|_w = 0$ .

A semi-implicit time-marching algorithm was used to solve the system of equations. By marching in time until all quantities (velocity components and volume fraction) converged to one part in 100,000, a steady-state solution was reached.

#### 4.2 Flow Between Parallel Plates

The first problem considered is flow between two parallel plates separated by  $6.35\text{E-}3$  m (0.25 in). A homogeneous 50-50 mixture (by volume) enters the gap uniformly with a velocity of 0.01 m/s. Other characteristics are shown in Table 1. By the time the flow reaches the exit, a fully developed situation exists.

Figure 1 shows the fully developed velocity profiles for the binder ( $v_1$ ) and the particles ( $v_2$ ). The differences in the velocity distribution must be

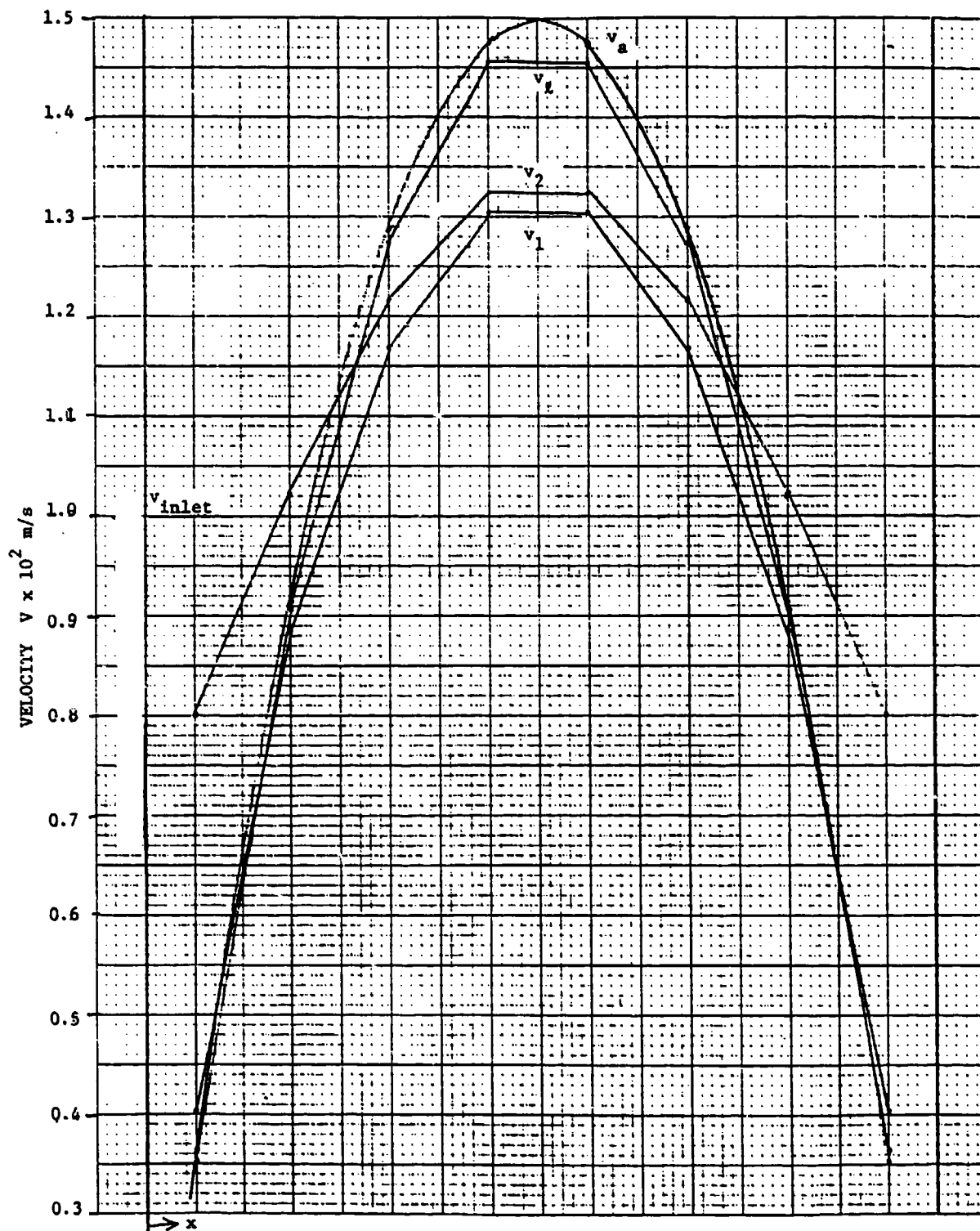


Fig. 1. Fully Developed Flow Between Parallel Plates

**TABLE 1. Flow Between Parallel Plates**

Gap	6.35E-3 m (0.25 in)
Inlet velocity $v_1 = v_2$	0.01 m/s
Inlet $\theta_1$ (binder)	0.5
$\theta_2$ (particles)	0.5
$\mu_1 = \mu_2$	200 Pa-s
$\rho_1 = \rho_2$	1000 kg/m <sup>3</sup>
$K_{12}$	1.0E8 Pa-s/m <sup>2</sup>
Re	3.175E-4

entirely due to the different boundary conditions imposed on the 2 components because the material properties used are the same. This was verified by running a problem where both components had no slip boundaries and this yielded the fully developed velocity profile  $v_g$  shown in Fig. 1 for both components. For reference, the well known parabolic velocity profile is also shown and labeled  $v_g$  in Fig. 1. Note that the velocity distributions of both the binder and the particles are flatter than the reference case. The particle velocity is consistently higher than the binder velocity throughout the cross-section.

Figure 2 shows the volume fraction distribution of binder ( $\theta_1$ ) and particles ( $\theta_2$ ). It is readily apparent that a partial separation of components has occurred. The particles have a relative maximum concentration in the center of the gap while the binder is more concentrated near the wall.

It is worth noting that this separation phenomena is due entirely to the difference in velocity boundary conditions at the wall for the two components.

#### 4.3 Annular Flow

The second problem considered is two-dimensional axisymmetric flow between two concentric cylindrical surfaces forming an annular region. The problem characteristics are summarized in Table 2. The inner radius is

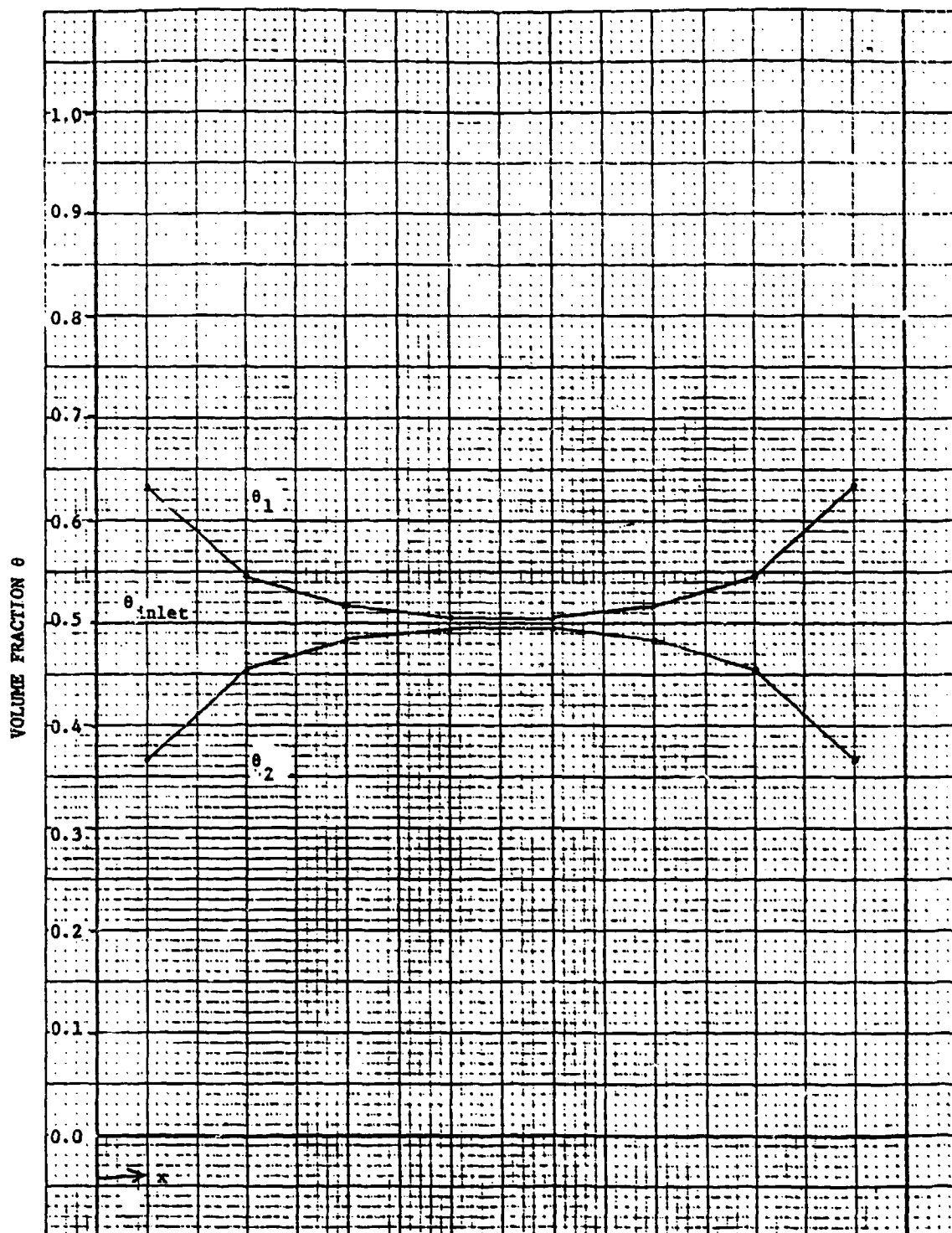


Fig. 2. Fully Developed Volume Fraction Distribution for Flow Between Parallel Plates



TABLE 2. Flow Into Annulus

$R_{in}$	0.01905 m (0.75 in)
$R_{out}$	0.0254 m (1.0 in)
Gap	6.35E-3 m (0.25 in)
Inlet velocity $v_1 = v_2$	0.01 m/s
$\theta_1$ (binder)	0.2242
$\theta_2$ (particles)	0.7758
$\mu_1 = \mu_2$	200 Pa-s
$\rho_1$ (binder)	920 kg/m <sup>3</sup>
$\rho_2$ (particles)	1950 kg/m <sup>3</sup>
$K_{12}$	1.0E8 Pa-s/m <sup>2</sup>

0.01905 m (0.75 in) and the outer radius is 0.0254 (1.0 in). This results in a 6.35E-3 m (0.25 in) annular gap. Here, we have used a homogeneous mixture with a higher particle volume fraction (.77) and a material density difference between the binder (920 kg/m<sup>3</sup>) and particles (1950 kg/m<sup>3</sup>).

Figure 3 shows the fully developed velocity profiles. The velocity distribution when both components have no slip boundary conditions is labeled  $v_e$ . This solution is similar to the parallel plates solution except the central peak velocity occurs nearer the inner surface. The particle velocity ( $v_2$ ) is consistently higher than the binder velocity ( $v_1$ ) throughout the cross-section. Due to the higher particle concentration and material density, the velocity profiles are flatter and maximum velocities less than the corresponding results for the parallel plates.

The volume fraction distributions are shown in Fig. 4. The particle volume fractions ( $\theta_2$ ) show the highest value near the middle and lower near

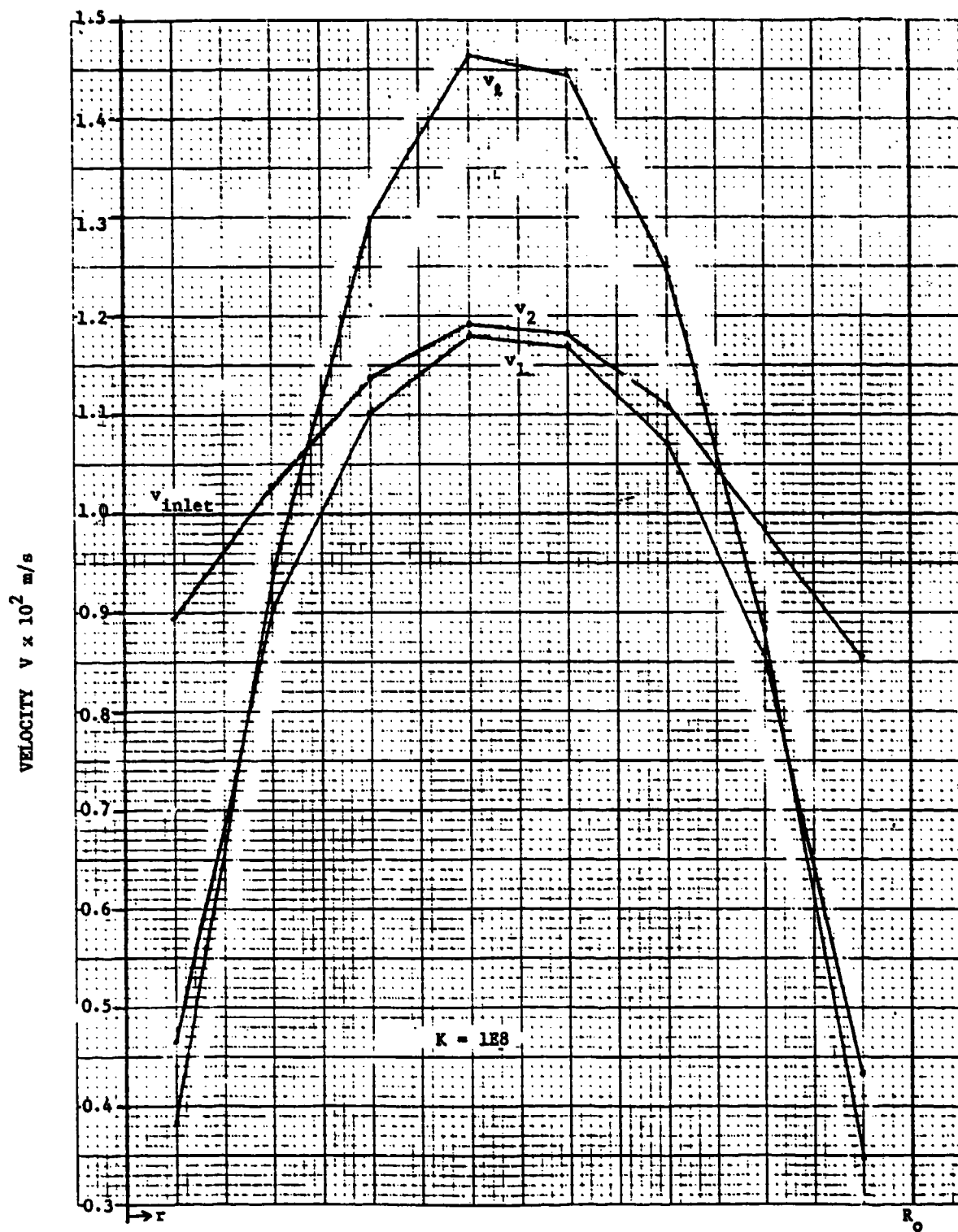


Fig. 3. Velocity Distribution in Fully Developed Annular Flow

VOLUME FRACTION  $\phi$

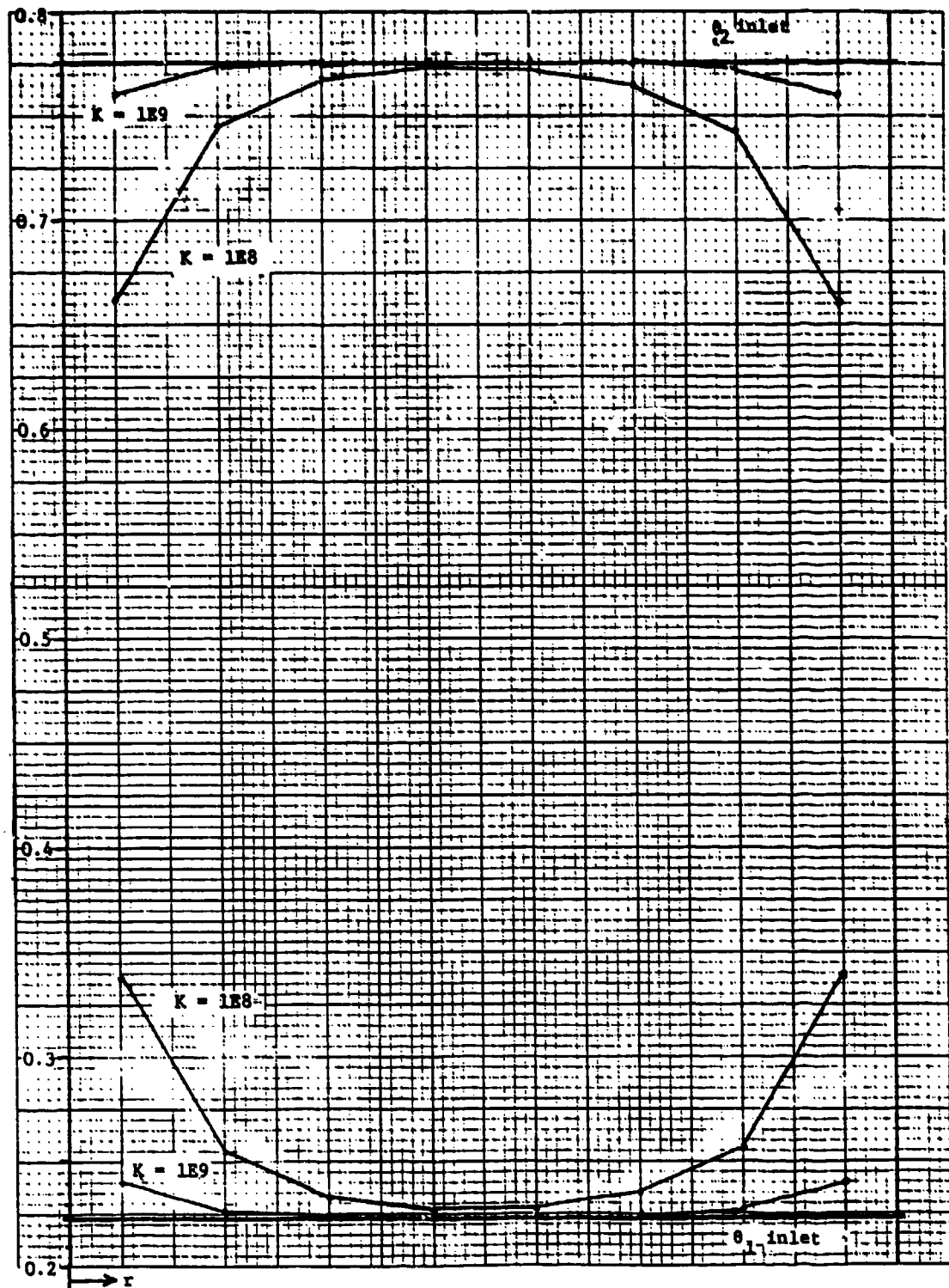


Fig. 4. Volume Fraction Distribution in Fully Developed Annular Flow

the walls. The interfacial drag coefficient ( $K_{12} = 1.0E8 \text{ Pa-s/m}^2$ ) is the same as used in the parallel plates case. In addition, two other runs were made with  $K = 1.0E9$  and  $K = 7.0E10$ . The results are shown in Fig. 4 where for  $K$  greater than  $1.0E10$  the separation becomes very small.

## 5. DISCUSSION OF EXPERIMENTAL MEASUREMENTS FOR TRANSPORT PROPERTIES

The following transport properties are needed for the system with a binder and 2 different sizes of particles under consideration so that the set of governing equations with appropriate initial and boundary conditions can be solved.

- (1)  $\mu_m$  needs to be measured vs shear rate and time at the processing temperature.\*
- (2)  $D_{2m}$  and  $D_{3m}$  to be measured if possible.
- (3)  $f_2$  and  $f_3$  shear lift force and gravity force, can be computed (please see Section 5.3).
- (4)  $F_{21}$  and  $F_{31}$  can be estimated (please see Section 5.4).

It is recognized that the transport properties are a function of composition of materials and time history. We recommend that the time history and temperature dependence may be included in some measurements if this can be conveniently done.

### 5.1 Viscosity Measurements

It is recommended that viscosity be measured with the following compositions, with respect to time and shear rate:

- (1) Binder only
- (2) Binder + particle 2 (p2) with p2 at 1/3 nominal value.  
Binder + p2 with p2 at 2/3 nominal value.

---

\*It is assumed that  $\tau$  is a function of velocity gradient and mixture viscosity--Non-Newtonian fluid.

Binder + p2 with p2 at full nominal value.

(3) Binder + particle 3 (p3) with p3 at 1/3 nominal value.

Binder + p3 with p3 at 2/3 nominal value.

Binder + p3 with p3 at full nominal value.

(4) Binder + p2 + p3, both p2 and p3 at nominal value.

The viscosity  $\mu$  of a fluid, in general, exhibits shear rate dependence and can be characterized as follows

$$\mu_m = K \left| \frac{\partial W}{\partial r} \right|^n$$

where  $K$  is an empirical constant and  $|\partial W/\partial r|$  is the shear rate. The exponent  $n$  accounts for various rheological behaviors of the fluid.  $n = 0$  for a Newtonian fluid;  $n > 0$  for a shear thickening fluid, that is, a viscosity which increases with shear rate; the reverse is the case of  $n < 0$ , a shear thinning fluid. Depending on the shear rates and the particle size, internal friction or collision, a given fluid may exhibit both ranges of behavior[11]. For the case of a shear thickening fluid ( $n = 1$ )

$$K = C_\mu \theta_p^2 a^2 \phi_p$$

where  $C_\mu$  is a constant ( $= 1$  for spheres having elastic collision),  $\theta_p$  is the volume fraction of particles with radius  $a$ [1].

## 5.2 Diffusivity Measurements

It is recognized that diffusivity cannot be obtained by direct measurement. Therefore, this information may be obtained indirectly through densitometry of particle distributions and photoelasticity of stress measurement of slices from solid propellant specimens. We recommend that these measurements be made at the compositions as outlined in (1) of viscosity measurements. Experimental data is needed, but for a shear thickening fluid ( $n = 1$ ), the particle diffusivity is given by

$$D_{km} = C_d \left( \frac{\rho_m}{\rho_k} \right) \left( \frac{a^2}{\theta_k^3} \right) \left| \frac{\partial W}{\partial r} \right|, \quad k = 2, 3$$

where  $C_d$  is a coefficient of the order of 10[7].

### 5.3 Field Forces $f_2$ and $f_3$

These include gravity  $g$ , and shear lift forces. The former is negligible for the present case, and the latter has been given analytically for spheres. It will be determined with semi-empiricism in the course of computation by validation from particle density distributions and shear stress distributions in the solid propellant if available. It is given for a spherical particle[3,7] by

$$f_k = C_1 [3(6.46)/4\pi] (\rho_m/\rho_k) \left[ \nu \left( \frac{\Delta W}{a} \right)^2 \left| \frac{\partial W}{\partial r} \right| \right]^{1/2}$$

where  $W$  is the velocity outside the boundary layer,  $\Delta W = W - W_k$ , the velocity difference between the fluid and the particle,  $a$  is the particle radius, and  $(\partial W/\partial r)$  is the shear rate of the layer. The coefficient  $C_1$  accounts for non-sphericity. Lifting of larger particles by shear motion of small particles will be dealt with in a later report.

### 5.4 Inverse Relaxation Time

Inverse relaxation times are predictable for spherical particles. For the present application, iteration with empirical coefficients and validation by final particle density distributions can yield semi-empirical modifications for predictive purposes. For particle 2,  $F_{21}$  is given by

$$F_{21} = C_F \frac{7.5 \theta_2 \bar{\mu}}{2a^2 [\rho_2 + (\rho_m/2)]}$$

where  $C_F$  is an empirical coefficient,  $\theta_2$  is the volume fraction of particles 2,  $\bar{\mu}$  is the fluid viscosity, and  $a$  is the radius or characteristic dimension of the particle[1].

If all the items in Sections 5.1 and 5.2 can be furnished, they will be most helpful. The order of priority should be

- (1) Viscosity measurements.
- (2) Densitometry of particle distribution of sliced solid specimens.
- (3) Photoelasticity of sliced solid specimens.

The minimum measurement would be flow through a tube and measure the flowrate and pressure drop, from which the viscosity and non-Newtonian parameters can be deduced. We can proceed with results from Item (1) alone. The effort toward achieving a realistic computer program will be facilitated or reduced by having Items (1) and (2), and more so if Item (3) is available.

## 6. DISCUSSIONS AND CONCLUSIONS

A continuum approach to the modeling of a dense suspension has been taken as opposed to discrete particle tracking. Within the continuum approach, two formulations have been identified: the multifluid model, and the diffusion model. While the multifluid model is more complete, there are more unknown coefficients associated with the model and these coefficients need to be determined. The single velocity diffusion model is computationally more economical and it involves relatively fewer unknown coefficients than the multifluid model. Correspondence between the two models has been pointed out.

A crucial feature needed in the mathematical model is the ability to predict partial component separation from a homogeneous mixture. The only way the single velocity diffusion model can predict partial separation is from the shear lift field force term. The magnitude of this term must be determined experimentally. Due to the current lack of detailed and reliable experimental data, approximations were made for the interaction terms in the multifluid model. Even in the absence of a shear lift field force, the multifluid model can predict partial component separation by having different component velocity boundary conditions at the wall.

In summary, our preliminary investigation of flow modeling during solid propellant processing has yielded the following conclusions:

1. Meaningful prediction of concentration distribution of components can be obtained from computations with a minimal acquisition of transport properties at the initiating phase. These preliminary predictions can be used to guide experiments which are urgently needed to quantify the transport properties and to validate the mathematical models.
2. Currently, the multifluid model and the single velocity diffusion model are viewed as being complementary. While the multifluid model can be used to gain insight into the underlying individual physical mechanisms, the diffusion model gives global phenomenological behavior of the system. The interrelations between the two mathematical models have been clarified. It is anticipated that at a later date, depending on availability of the needed experimental data and understanding of physical mechanisms, we shall select one of the two models as the reference predictive tool.
3. Validation of computed concentrations can be made by sections of solidified models or checked by burning rates for uniformity of pressure.
4. Exploratory calculations have shown the ability of the multifluid model to compute partial separation of components by boundary condition differences. More parametric study can be done to give insight into the sensitivity of the various empirical coefficients.
5. The problem under investigation is important, but very difficult. The preliminary results from the present study lays the foundation for the future work and it appears that useful results can be obtained.



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